

go over projectile questions
 free body diagram worksheet
 take home lab simulation activity
 shirley off cliff at 4.0 m/s 35.0 degrees
 above the horizontal

$$v_{yi} = 4 \times \sin(35) = 2.294305745404184$$

$$v_x = 4 \times \cos(35) = 3.276608177155967$$

$$a = -9.80 \text{ m/s}^2$$

$$d = -10.0 \text{ m}$$

$$d = \frac{1}{2}gt^2 + v_{yi}t$$

$$-10 = -4.9t^2 + 2.294t$$

$$\checkmark 14.187$$

$$t = \frac{-2.294 \pm \sqrt{2.294^2 - (4 \times -4.9 \times 10)}}{-9.8}$$

$$t = \frac{-2.294 - 14.187}{-9.8} = 1.682 \text{ s}$$

$$dx = v_x t = 3.2766 \times 1.682 = 5.5112$$

$$= 5.5 \text{ m}$$

$$v_{yf} = v_{yi} + at = 2.294$$

$$+ (-9.8 \times 1.682) = -14.1896 \text{ m/s}$$

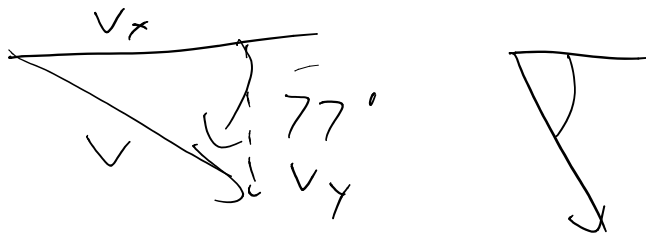
$$v_x = 3.2766 \text{ m/s}$$

$$v^2 = (14.1896^2 + 3.2766^2) =$$

$$v = 14.56 \text{ m/s}$$

$$\text{direction } \theta = \tan^{-1}(14.1896/3.2766)$$

$$= 77^\circ \text{ below horizontal}$$



Quiz October 17th vectors and projectiles

p63

Q45

$$d_x = 30.0 \text{ m}$$

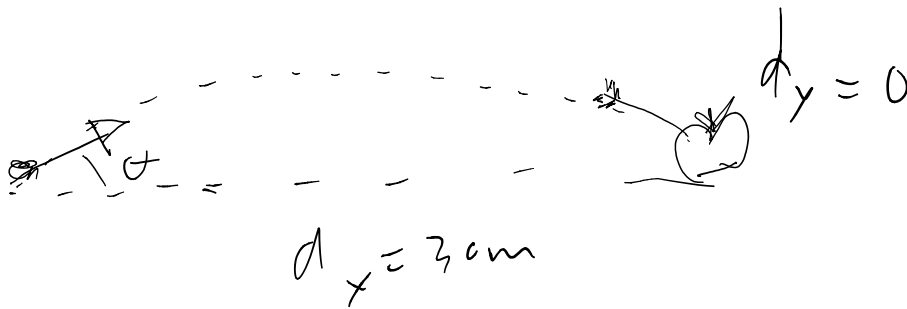
$$\text{horizontal } d_y = 0$$

$$\theta = ?$$

$$v = 35 \text{ m/s}$$

$$v_x = v \cos \theta$$

$$v_y = v \sin \theta$$



$$d_x = v_{xt} = 30 = v_{xt} = t = 30/v_x$$

$$d_y = \frac{1}{2}gt^2 + v_{yi}t = 0 = -4.9t + v_{yi}$$

sub in

$$0 = -4.9(30/v_x) + v_{yi}$$

$$v_{yi}v_x = 4.9 \times 30 = 147 = v^2 \sin q \cos q$$

trig identity $2 \sin q \cos q = \sin 2q$

$$147 = v^2 \frac{1}{2} \sin 2q$$

$$147 = (35)^2 \frac{1}{2} \sin 2q$$

$$0.12 = \frac{1}{2} \sin 2q$$

$$0.24 = \sin 2q$$

$$\sin^{-1} 0.24 = 13.887 = 2q$$

$$q = 6.9 \text{ degrees}$$

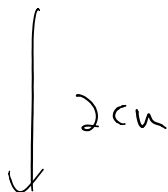
woohoo

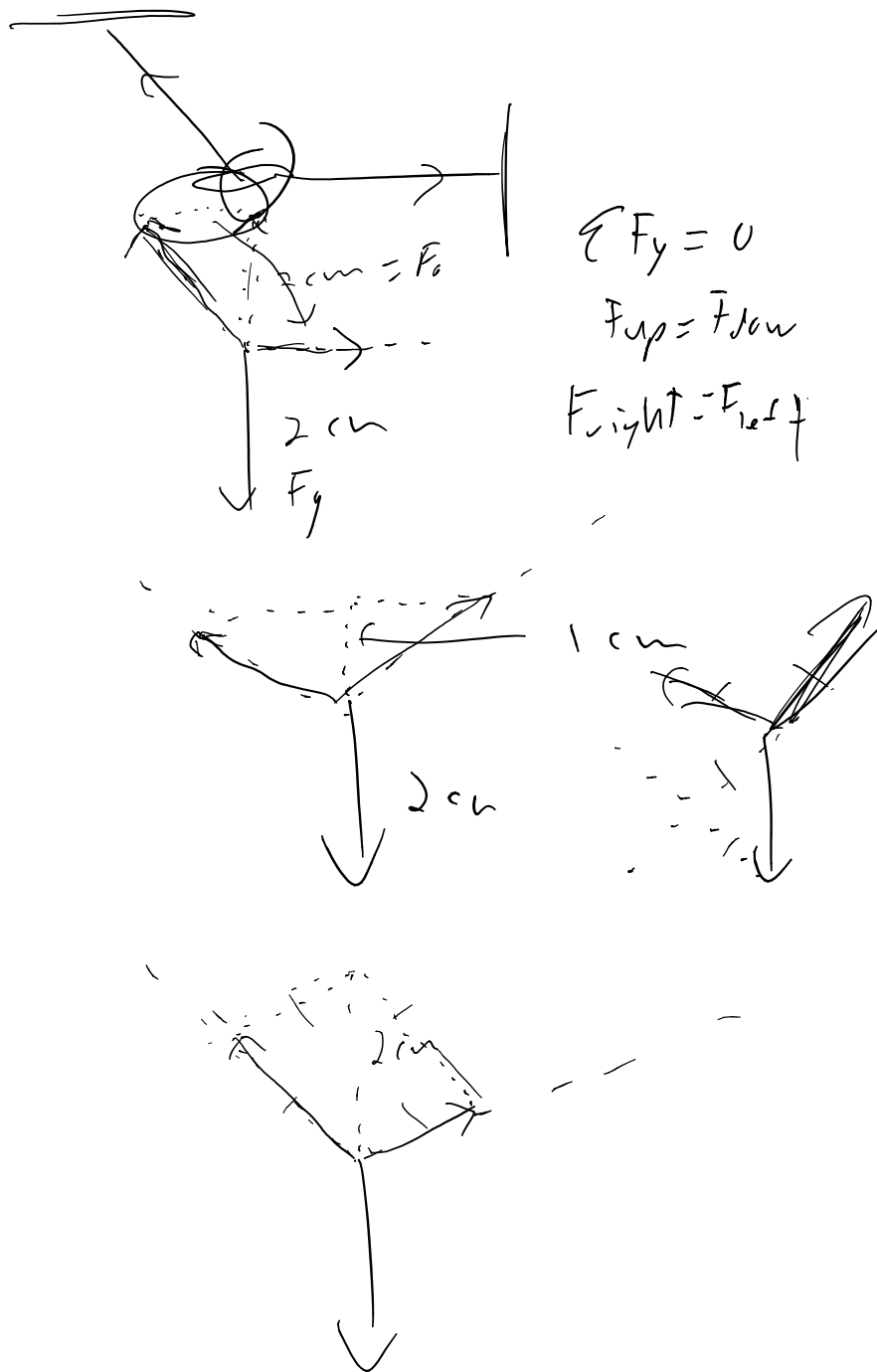
assignment

p64 Q55, 57, 59

Handouts:

1. play with a projectile motion applet at home on a computer
2. Free body diagrams - must be to scale use 2.0 cm for F_g





go over projectile questions
 free body diagram worksheet
 take home lab simulation activity

Fred, Ted and Ned jumped off the cliff.
 determine t , v , dx
 Ned jumps at 4.00 m/s at 35.0 degrees
 above the horizontal off a 10.0m high
 cliff.

break the problem into x and y motion
 $V_x = V \cos \theta$

$$v_y = v \sin \theta$$

$$v_x = 4 \cos(35) = 3.276608177155967$$

$$v_{yi} = 4 \sin(35) = +2.294305745404184$$

$$a = g = -9.80 \text{ m/s}^2$$

$$dy = -10.0 \text{ m}$$

$$d_y = \frac{1}{2} a t^2 + v_{yi} t$$

$$-10 = -4.9 t^2 + 2.2943 t$$

$$0 = -4.9 t^2 + 2.2943 t + 10$$

$$-b \pm \sqrt{b^2 - 4ac} / 2a$$

$$-2.294 \pm \sqrt{(2.294)^2 - 4(-4.9)(10)} / 2(-4.9)$$

$$t = 1.68174 \text{ s} = 1.68 \text{ s}$$

$$d_x = v_x t = 4 \cos 35 \times 1.68 = 5.5 \text{ m}$$

$$v_y = at + v_{yi} = (-9.8 \times 1.68174) + 2.294$$

$$= -14.18705$$

$$v = \sqrt{v_x^2 + v_y^2} = \sqrt{3.277^2 + 14.187^2}$$

$$v = 14.56 \text{ m/s}$$

direction:



$$\theta = \tan^{-1} \frac{v_y}{v_x}$$

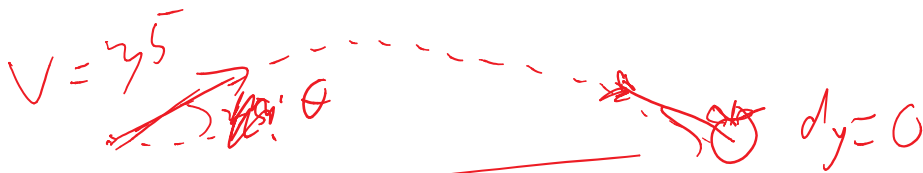
$$\theta = \tan^{-1} \frac{14.19}{3.27}$$

$$v = \frac{1 \text{ cm} \cdot 14.11}{3.27}$$

$$\theta = 77^\circ \text{ below horizontal}$$

$$\phi = 13^\circ \text{ from vertical}$$

p63
Q45

$$v = 25 \text{ m/s}$$


$dy = 0$

$$d = 30 \text{ m}$$

$$d_x = v_x t + \left(d_y + \frac{1}{2} a t^2 + v_{y,i} t \right)$$

$$t = \frac{d_x}{v_x}$$

$$0 = \frac{1}{2} g t^2 + v_{y,i} t$$

$$0 = \frac{1}{2} g t^2 + v_{y,i}$$

$$0 = (-)4.9 \left(\frac{30}{v_x} \right) + v_{y,i}$$

$$0 = (-)4.9\left(\frac{30}{v_x}\right)^2 + v_{yi}$$

$$v_{yi} v_x = 4.9(30)$$

$$v \sin \theta \quad v \cos \theta = 147$$

$$v^2 \sin \theta \cos \theta = 147$$

identity $\textcircled{2} \sin \theta \cos \theta = \frac{\sin 2\theta}{2}$

$$v^2 \frac{\sin 2\theta}{2} = 147$$

$$(35 \text{ m/s})^2 \frac{\sin 2\theta}{2} = 147$$

$$\frac{\sin 2\theta}{2} = 0.12$$

$$\sin 2\theta = 0.24$$

$$2\theta = \sin^{-1} 0.24$$

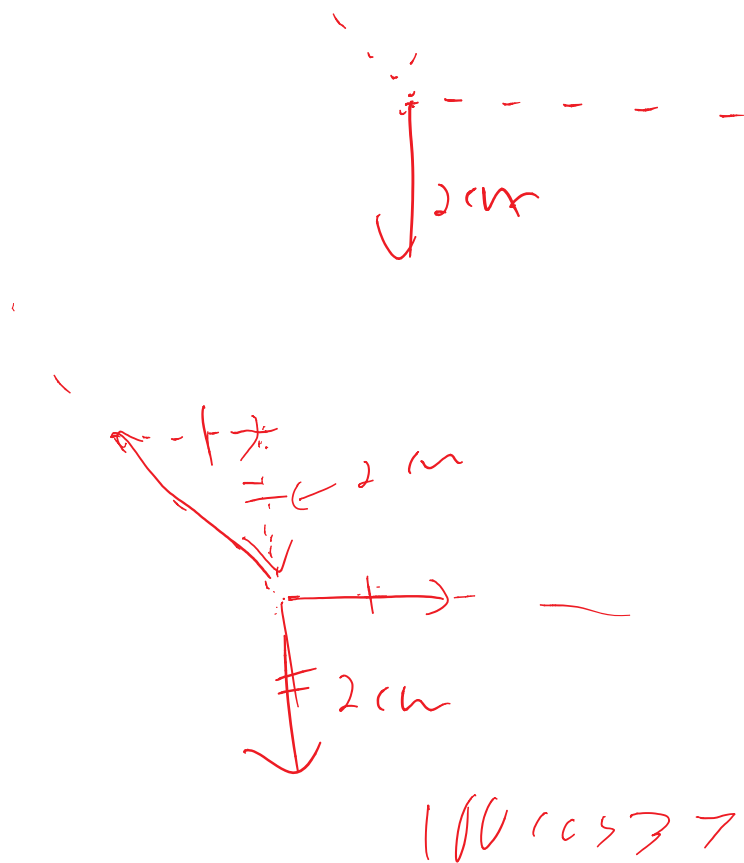
$$2\theta = 13.8^\circ$$

$$\theta = 6.9^\circ$$

do the projectile sheet first-
check next class
free body diagrams

CHECK NEXT CLASS
free body diagrams

make $F_g = 2.0$ cm and draw
the force vectors to scale



Q 47 a) $V_x = 79.86355$

$$V_{y_i} = 60.1815$$

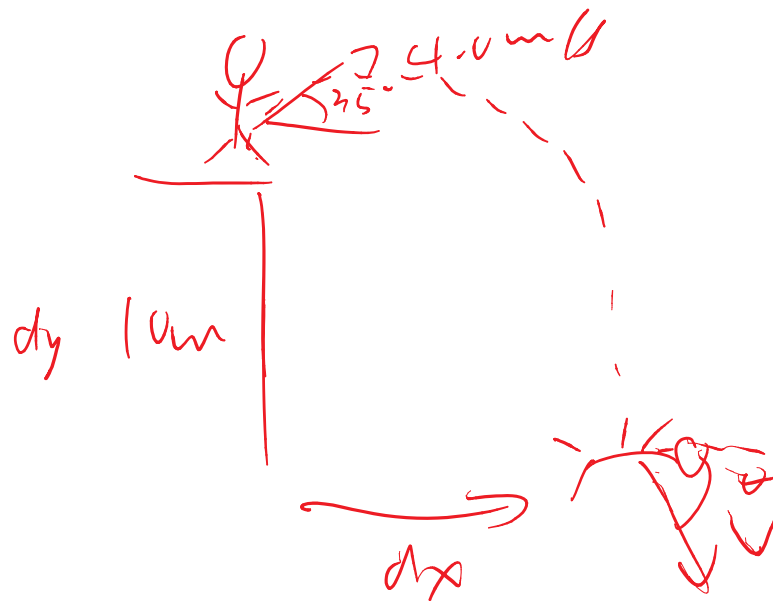
$$V_{y_f}^2 = V_{y_i}^2 + 2(-9.8)(-140)$$

$$V_{y_f} = 79.786$$

$$V = \sqrt{79.786^2 + 79.86^2}$$
$$= 112.88$$

113 m/s

angela, edward ran,
Mr. K. jumped off the 10.0m high cliff at
4.00m/s at 35.0degrees above the horizontal.
determine t, dx, v and θ



separate the problem into x and y components

x motion is constant velocity $d_x = v_x t$

y motion is constant acceleration, $g = 9.80 \text{ m/s}^2$

4 equations $d_y = \frac{1}{2}gt^2 + v_{yi}t$

$$v_y = gt + v_{yi}$$

$$v_y^2 = v_{yi}^2 + 2gd_y$$

$$v_{yi} = v \sin \theta = 4 \times \sin(35) = 2.294305745404184$$

$$v_x = v \cos \theta = 4 \times \cos(35) = 3.276608177155967$$

$$d_y = -10.0 \text{ m}$$

$$a = g = -9.80 \text{ m/s}^2$$

d_y

$$d_y = \frac{1}{2}gt^2 + v_{yi}t$$

$$-10 = -4.9t^2 + 2.2943t$$

quadratic

$$t = \frac{-(-2.294) \pm \sqrt{(-2.294)^2 - 4(-4.9)(-10)}}{-9.8}$$

$$t = 1.68s$$

$$dx = v \cos \theta t = 3.2766 \times 1.68s = 5.5m$$

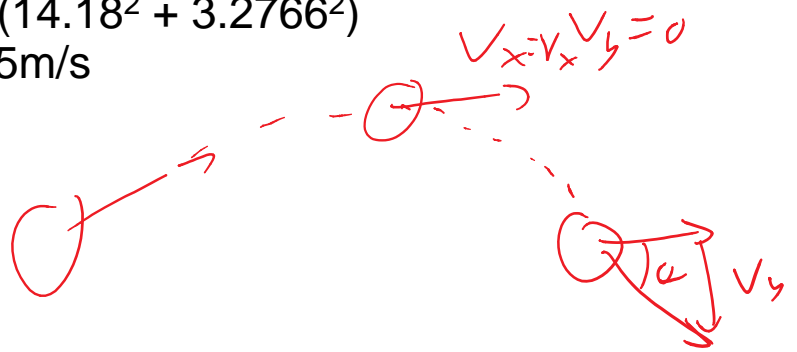
$$v_{yf} = v_{yi} + at = 2.294 + 9.8(1.68) = 14.18m/s$$

$$v_x = 3.2766$$

$$v = \sqrt{v_x^2 + v_y^2}$$

$$v = \sqrt{14.18^2 + 3.2766^2}$$

$$v = 14.55m/s$$



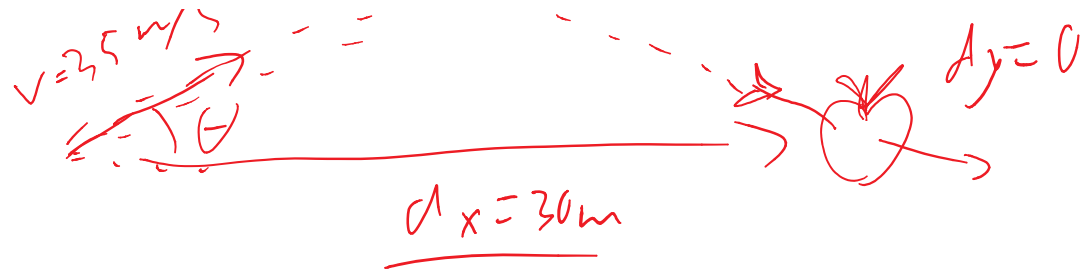
$$\theta = \tan^{-1} \frac{v_y}{v_x}$$

$$\theta = \tan^{-1} \frac{14.18}{3.27}$$

$$\boxed{\theta = 77^\circ \text{ below horizontal}}$$

Q36 p63 or 45





$$d_x = V_x t \rightarrow t = \frac{d_x}{V_x}$$

$$d_y = V_{yi} t + \frac{1}{2} g t^2$$

$$0 = \frac{V_{yi} t}{t} + \frac{\frac{1}{2} g t^2}{t}$$

$$0 = V_{yi} + \frac{1}{2} g t$$

$$0 = V_{yi} + \frac{1}{2} g \left(\frac{d_x}{V_x} \right)$$

$$-V_{yi} = \frac{1}{2} g \frac{d_x}{V_x}$$

$$-2 V_x V_{yi} = g d_x$$

$$\text{Range } d_x = \frac{-2 V_x V_{yi}}{g} \quad \text{if } \underline{d_y = 0}$$

$$-2 (V \cos \theta) (V \sin \theta) = 9.8 (30)$$

$$-2 (\cancel{V^2}) \cos \theta \sin \theta =$$

$$\underline{2 \cos \theta \sin \theta = \frac{9.8 (30)}{35^2}} \quad \uparrow V^2$$

trig identities $2 \cos \theta \sin \theta = \sin(2\theta)$

$$\sin(2\theta) = 9.8 \times 30 / 35^2$$

$$\sin(2\theta) = 0.24$$

$$2\theta = \sin^{-1}(0.24)$$

$$\theta = 13.8865/2 = 6.9433 \text{ degrees}$$

$$(\text{or } 90 - 6.9 = 83.1)$$

you can solve by $v_x^2 + v_y^2 = v^2$

Assignments:

1. worksheet explore projectiles in a simulation
2. worksheet draw free body force diagrams to scale with F_g of the rock at 2.0 cm and other forces to scale.

